Investigation on aerodynamic performance of H-type darrieus vertical axis wind turbine with different series airfoil shapes

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Article history:
Received 25 December 2022
Received in revised form 05 March 2023
Accepted 18 June 2023

Keywords:
H-type
DMST
Power Coefficient
Tip Speed
Self-starting

ABSTRACT

Wind energy is one of the most important renewable energies since it reduces environmental pollution. Darrieus VAWTs with straight blades are more prevalent in small-scale power generation due to their simple blade design and easy construction. The investigation of the performance of VAWTs is a topic that is fascinating for researchers to look into. Researchers have paid special attention to the Double Multiple Stream tube (DMST) models for VAWT simulation because of the good correlation between the DMST model and the experimental results. In this paper, double multiple stream-tube analysis is performed using MATLAB programming to predict the aerodynamic performance of H-type Darrieus fixed pitch VAWT, more specifically, the power coefficient (Cp) and the tip speed ratio (TSR). The fact that the H-type Darrieus rotor has poor self-starting despite having a good power coefficient which is a constant worry at low wind speeds. The selection of the air foil is one of the most essential factors to take into account while trying to enhance the aerodynamic performance of H-type Darrieus fixed pitch VAWT. In this study, first, results from experiments were used for the validation of the model, and then, 4 different families of symmetrical airfoils were compared. The results indicate that the symmetrical airfoil S-1046 showed exceptional aerodynamic performance and a high starting torque for a low wind speed of 4 m/s.

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1. Introduction

In the current world of technological advancements, innovations, and inventions, industrialization is reaching new heights. Technological progress is inextricably linked to the use of energy. In contrast, rapid industrialization has created a slew of problems and challenges that are far too significant to ignore now. The issues to be considered are increasing air pollution, rising fuel costs, massive energy consumption in various industries, etc. [1]. The selection of suitable alternative energy sources is a significant issue impacting economic growth worldwide. The wind is considered a source of alternative energy because it is renewable, economically competitive, relatively clean, and environmentally friendly.

Wind technology transforms kinetic energy from the wind into mechanical or electrical power through wind turbines (WTs) using aerodynamically designed blades [2]. WTs can be divided into two categories, horizontal axis wind turbines (HAWTs) and vertical axis wind turbines (VAWTs), depending on the orientation of the axis of alignment [3]. HAWTs rotational axes are parallel to the wind stream, and they were a popular choice due to their better aerodynamic behaviour and efficiency on a large scale. In contrast, VAWTs’ rotational axes are perpendicular to the wind stream. VAWTs have many benefits that guide researchers’ attention. VAWTs are omnidirectional without needing a yaw system, which results...
in fewer hydrodynamic motions and platform design constraints. The generator location of VAWTs differs from that of HAWTs, which are located at the base of the tower, reducing the load on the tower. This type of design has a direct effect on the turbine’s easy maintenance, construction, and installation [4]. Many VAWT designs have been created over the years and can be categorized into drag-type (Savonius VAWTs, which are the simplest sort) and lift-type (Darrieus VAWTs, which are more complicated) based on rotation-driving aerodynamic forces [5].

Typically, there were two types of Darrieus rotors: curved and straight-bladed. Darrieus VAWTs with curved blades have lower bending stress in the blades than Darrieus VAWTs with straight blades; hence, they are more economically successful [6]. However, Darrieus VAWTs with straight blades are more common in small-scale power generation due to the ease of their blade design [7]. Straight-blade VAWTs are Darrieus VAWTs with straight blades instead of curved blades. As a result of its rotor aspect, it is always referred to as H-rotor [8]. In recent years, H-type Darrieus VAWTs are getting more notice in the field of wind energy. In many countries, H-type Darrieus VAWTs are actively researched and promoted. They work well in turbulence and different environments and regions [9]. Darrieus VAWTs have complex aerodynamic behavior, but different numerical models for performance prediction and design exist. These models are classified as momentum, vortex, and computational fluid dynamics (CFD) models in the literature. For this paper, a momentum model is chosen to predict VAWT’s performance using a double multiple stream tube (DMST) models. The momentum models, also known as streamline (ST) models, investigate the dynamic properties of the airflow on the blades and their forces. These models concentrate on the momentum (actuator disk) theory and can be broken down further into the following categories: (single (S), multiple (M), and double multiples (DM)) stream tube models. Templin, R. [10]. Created SST model and calculated momentum balance using a single stream tube that encompassed the entire turbine, and flow velocities in the stream tube were assumed to be uniform. This model’s many assumptions cause inaccurate performance predictions and higher prediction numbers. Strickland, J. [11]. Developed MST model, which is a more complex analytical method than SST. He assumed that the induced velocity varies vertically and horizontally across the frontal disc area of the rotor. Airfoil geometry, drag forces, curvature flow, etc., have been counted in this model.

The generator location of VAWTs differs from that of HAWTs, which are located at the base of the tower, reducing the load on the tower. This type of design has a direct effect on the turbine’s easy maintenance, construction, and installation. Many VAWT designs have been created over the years and can be categorized into drag-type (Savonius VAWTs, which are the simplest sort) and lift-type (Darrieus VAWTs, which are more complicated) based on rotation-driving aerodynamic forces. Darrieus VAWTs have the highest efficiency value, but they have poor self-starting capability, which can be avoided through careful design. Many projects related to the Darrieus turbine have been studied through this project to improve and develop the study of the H-type Darrieus turbine. Durrani et al. [14]. Compared the performance of NACA 4-digit symmetric airfoils (0012, 0015, and 0018) and NACA 0022 (a thicker airfoil size) for a three-blade VAWT at various wind speeds. The results show that, at the various tip speed ratios, NACA0015 gives a more steady performance than the others. Castillo, J. [15], studied many parameters for designing small-scale VAWT with solid wood as a construction material, such as type of blade profile, number of the blade, rotor radius, TSR, and chord length. He used the DMST model for rotor aerodynamic analysis based on a Matlab program. He analyzed the effect of the blade profile on the symmetric NACA0015, and NACA 0021. He concluded that the rotor with the thicker airfoil NACA 00021 has a higher self-starting ability. Mohamed, M. [16]. Studied the aerodynamic performance of the H-rotor Darrieus VAWT by using 2D-CFD simulations to study the effect of airfoils on power coefficient. He studied the effects of 20 different airfoils (symmetric and asymmetric) and demonstrated that the use of the symmetric S-1046 airfoil increases the output power of the H-rotor Darrieus turbine. Kanyako and Janajreh [17]. Tested different types of airfoils numerically using 2D-CFD simulation for a small-scale VAWT with straight-bladed with a solidity of 0.98 to obtain the best possible performance. They concluded that the best
sectional profile airfoil at low speeds was NACA 0015. Nguyen et al. [18] numerically analyzed the effect of airfoil geometry, the starting azimuth angle of the blade, and wind velocity on self-starting behavior for a 1 KW H-Darrieus rotor with three blades. They analyzed the effect of airfoil thickness on the symmetric NACA 4-digit (0012, 0015, 0018, 0021). They concluded that the H-Darrieus rotor with the thinner airfoil NACA 0012 has a lower self-starting ability, whereas the rotor with the thicker airfoil NACA 00021 has a higher self-starting ability. Subramanian et al. [19]. Numerically investigated the effect of different airfoil profiles on the performance of VAWTs. They discovered that at various tip-speed ratios, different airfoils with different profiles behave differently. Thicker airfoils operate better for lower tip-speed ratios, whereas thinner airfoils work better for higher tip-speed ratios.

In this study, numerical code was developed based on the DMST model with variable interference factors using the MATLAB program to compare the performance and torque characteristics of H-type Darrieus WTs. Although the aerodynamic performance of different airfoil profiles to improve the self-starting performance of small-scale fixed-pitch H-type Darrieus WTs was also studied.

2. Material and method

2.1 Aerodynamic analysis of H-type Darrieus VAWT

DMST model illustrated in Fig. 1 is an analytical model used for Darrieus VAWTs with curved blades for determining aerodynamic blade loads and rotor performance, which was developed by I. Paraschivoiu [20]. The rotor’s upstream and downstream sides have their induced velocity. The pressure discontinuity causes the wind speed to slow, resulting in an induced velocity. The upstream-induced velocity \( V_{up} \), which is the axial flow velocity that passes through the stream tubes, and the downstream-induced velocity \( V_{do} \) are calculated as follows:

\[
V_{up} = a_{up} V_o \quad (1)
\]

\[
V_{do} = a_{do} V_o \quad (2)
\]

where \( a_{up} \) and \( a_{do} \) are upstream and downstream interference factors, respectively, and it is taken that \( 1 > a_{up} > a_{do} > 0 \) and their value drops as the tip speed ratio increases. The value of \( a_{up} \) can be determined iteratively by starting with an assumption of \( a_{up} = 1 \). After that, \( a_{up} \) can be determined iteratively starting with \( a_{do} = a_{up} \). \( V_o \) is ambient air velocity, and \( V_e \) is equilibrium velocity at the middle plane, which is affected by the upstream wake velocity: and it is less than \( V_{up} \) but greater than \( V_{do} \) because the induced velocity in the axial stream tube reduces as given by calculated as follows:

\[
a_{up} = \frac{V_{up}}{V_o} \quad (3)
\]

\[
a_{do} = \frac{V_{do}}{V_o} \quad (4)
\]

\[
V_e = (2V_{up} - V_o) V_o = (2a_{up} -1) V_o \quad (5)
\]

by substituting equation 5 into equation 2, equation 6 is yield.

\[
V_{do} = a_{do} (2a_{up} -1) V_o \quad (6)
\]

the DMST model for H-type Darrieus VAWT, whose illustration is shown in Fig. 2, was adapted based on the following assumptions: (i) assumed that straight vertical blades were subject to the constant flow velocity across the entire length despite the Troposkien-shaped Darrieus turbine used by Paraschivoiu; therefore, angle (\( \delta = 0 \)). (ii) Assumed that VAWT is fixed-pitch, utilizing symmetric airfoils, where the line of the chord is tangent to the blade flight path, and \( a_{do} = 0 \). (iii) 36 stream tubes were employed, meaning wind conditions were evaluated in \( 5^\circ \) increments at blade positions. This number was used by Paraschivoiu to present his model's results [21, p. 164]. More stream tubes were tested to examine air conditions in smaller increments; however, the power coefficient and torque didn't change.

![Figure 1. The DMST model is shown schematically.](image)

![Figure 2. Two-bladed H-type Darrieus](image)
\[ \text{Re}_b = \frac{V_{up} c}{v} \]  

(10)

where \( c \) is the blade chord and \( v \) is air kinematic viscosity for air at the temperature of 15°C has a reference value of 1.4607*10^{-5} m²/s [22].

Finally, the upstream half-power coefficient \( C_{P,up} \) is calculated using:

\[ C_{P,up} = C_{Q,up,av} X \]  

(17)

where TSR is the tip speed ratio of the rotor, which is calculated as follows:

\[ X = \frac{\omega R}{V_{up}} \]  

(18)

and \( C_{Q,up,av} \) the average torque coefficient is calculated as follows:

\[ C_{Q,up,av} = \frac{Q_{up,av}}{\frac{1}{2} \rho \pi R^2 V_{up}^2} \]  

(19)

The rotor’s upstream side average torque \( (Q_{up,av}) \) is given by:

\[ Q_{up,av} = \frac{N}{2 \pi} \int_{-\pi}^{\pi} Q_{up}(\theta) d\theta \]  

(20)

where \( Q_{up}(\theta) \) is the torque produced by a blade, which is calculated by combining the lift and torque calculations.

\[ Q_{up}(\theta) = \frac{1}{2} \rho a c R L C_{T,up} V_{up}^2 \]  

(21)

The downstream side of the rotor is for the azimuth angle \((91 < \theta < 269)\) and using the same set of formulas, the average torque and power coefficient for the rotor downstream side are calculated as follows:

- Using \( V_{do} \) instead of \( V_{up} \), the downstream local relative velocity \( V_{r,do} \), local angle of attack \( \alpha_{do} \), and local tip speed ratio \( X_{do} \) can also be determined from equations 7, 8, and 9.
- Using double interpolation, \( \text{Re}_b \) and \( \alpha_{do} \) are utilized to obtain the appropriate drag \( C_d \) and lift \( C_l \) coefficients.
- Calculating downstream normal coefficients \( C_{N,do} \) and tangential coefficients \( C_{T,do} \).
- The downstream interference factor \( \alpha_{do} \) can be calculated after calculating the downwind flow conditions \( F_{do} \). The above procedure is repeated with the new value of \( \alpha_{do} \) until the initial and final \( \alpha_{do} \) values are similar.
- The average torque \( Q_{do,av} \) and power coefficient \( C_{P,do} \) on the downstream side are being calculated.

Finally, the rotor’s average torque and total power coefficient \( C_{P} \) are calculated by summing the two contributions:

\[ Q_{av} = Q_{up,av} + Q_{do,av} \]  

(22)

\[ C_{P} = C_{P,up} + C_{P,do} \]  

(23)

### 2.2 Numerical procedure

For the above referred for calculating aerodynamic loads, average torque \( Q_{av} \), and total power coefficient \( C_{P} \), a program code is developed by using MATLAB R2020a. Fig. 4 represents the procedure used for determining the torque and power coefficient for each blade position. The algorithm has 5 input design parameters of the rotor which are (rotor radius (\( R \)), blade length (\( L \)), number of the blade (\( N_b \)), chord length (\( c \)), blade profile), ambient air velocity (\( V_{in} \)), and rotational speed (\( \omega \)). Also, input from the airfoil’s data table such as lift and drag coefficient on Reynolds number and angle of attack is imported to the program to calculate rotor lift and drag coefficient by double interpolation. The value of airfoils data is calculated by summing the two contributions.

\[ C_{P} = C_{P,up} + C_{P,do} \]  

(24)
and $C_d$ in a different range of the Reynolds number (1, 8, 16, 36, 70, and 100)*10^4 and angle of attack from -180 to 180 degrees obtained from QBlade software. Were $C_l$ and $C_d$ extrapolated with the Montgomery method, with a CD90 at (1.6) value. Dynamic stall effects are not modeled present analysis code using DMST models. The average torque $Q_{av}$ and total power coefficient $C_P$ are the algorithm output captured by the integration of all the blade positions.

3. Results and discussion

3.1 Verifying the Model

For the validation of the model, two cases of WTs were used. The rotor’s parameter of the two types of turbines used to validate the model is given in Table 1. The reference data value was obtained by reading the plot using DigitizeIt software because the numerical results were unavailable.

In case I when comparing the present code analysis with the experimental analysis available in Ref. [23] shown in Fig. 5 it can be noticed that they match at low TSR but overshoot at higher TSR. There is an increasing difference between power coefficient values starting from TSR 2.5 until TSR 3.3, where the biggest difference in the value of $C_p$ is 0.1633 at TSR equal to 3.3. Nevertheless, the results from the experiment by Raciti Castelli, Englaro, and Benini in 2011 were an average of $C_p$, indicating that the experiment was conducted in multiple sets or trials. Since the real value of $C_p$ can vary on those varying trials or sets, this can affect the experimental graph analysis’s shape as well. In conclusion, the differences are still acceptable for both graphs since the two graphs no differ by more.

Table 1. Rotor’s parameters case I [23] and case II [24]

<table>
<thead>
<tr>
<th>Rotor parameters</th>
<th>Case I</th>
<th>Case II</th>
</tr>
</thead>
<tbody>
<tr>
<td>Blade profile</td>
<td>NACA0021</td>
<td>NACA0015</td>
</tr>
<tr>
<td>Blade number</td>
<td>3</td>
<td>2</td>
</tr>
<tr>
<td>Blade height</td>
<td>1.4564</td>
<td>6</td>
</tr>
<tr>
<td>Rotor radius</td>
<td>0.515</td>
<td>3</td>
</tr>
<tr>
<td>Chord length</td>
<td>0.0858</td>
<td>0.2</td>
</tr>
<tr>
<td>Test</td>
<td>$V=9m/s$</td>
<td>N=125rpm</td>
</tr>
</tbody>
</table>

Figure 5. Comparison DMST analysis code with experimental and numerical analysis (case I )

In contrast, the present code analysis graph and numerical analysis show a smaller difference at higher TSR. At TSR 2.33 the value of $C_p$ is 0.2465 which is the biggest value of $C_p$ between the present code analysis and numerical analysis than $0.2C_p$, and most importantly the two graphs are remarkably similar in shape.

In case II when comparing the present code analysis with the experimental analysis in Ref. [24] shown in Fig. 6 it can be noticed that the obtained result is great, where two graphs are similar in terms of their shape and curves as shown in Fig. 2. Both graphs peak at TSR 4.98 with the difference of 7.3%. In addition, the differences between them are very little and neglectable. In conclusion, the graph curve of the present code analysis simulation can replicate the shape from both numerical and experimental analysis and results agree well with those from other methods based on a variety of published findings. This can ensure that the present code analysis
using the DMST model provides a good and trusted result to evaluate the performance of H-type Darrieus wind turbine.

![Figure 6. Comparison DMST analysis code with experimental (case II)](image)

**3.2 Blade profile**

Many parameters, such as type of blade profile, number of the blade, rotor radius, blade length, chord length, and so on, affect the performance of H-type Darrieus WTs. The blade profile selection is the most critical parameter to improve the aerodynamic performance with the ability to self-start without needing additional components [25]. During the optimization process, the Blade profile’s impact on the power coefficient was considered, and the result is shown in the graphs. The simulation was conducted for four families of symmetric airfoils at low wind speed 4m/s and the results for the power coefficients of these profiles at different TSRs are shown. In this study, the chosen swept area will be 1.1 m². The characteristics of the H-type Darrieus wind turbine used for the present study using the DMST model are listed in Table 2.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rotor radius (R)</td>
<td>0.6875m</td>
</tr>
<tr>
<td>Blade height (L)</td>
<td>0.80m</td>
</tr>
<tr>
<td>Swept area (S)</td>
<td>1.10m²</td>
</tr>
<tr>
<td>Blade chord (c)</td>
<td>0.20m</td>
</tr>
<tr>
<td>Number of the blade (Nₜ)</td>
<td>4.00</td>
</tr>
<tr>
<td>TSR</td>
<td>2.00</td>
</tr>
<tr>
<td>Air velocity (Vₒ)</td>
<td>4.00m/s</td>
</tr>
</tbody>
</table>

**Table 2. Characteristics of H-type Darrieus WT used for the present study.**

![Figure 7. Cp vs. TSR for NACA-Family](image)

**3.2.2 S-Family**

In this family, compared the performance of symmetric airfoils (S1014, S1016, S1046, and S1048) as shown in Fig. 8 it can be seen that S1046 has a maximum power coefficient of 0.3342 at TSR 2 and has a higher self-starting ability compared with other airfoils in S-families.

![Figure 8. Cp vs. TSR for S-Family](image)

**3.2.3 FX-Family**

In this family, compared the performance of symmetric airfoils (FX 76-100, FX 76-120, FX 77080, FX 70-L-100, and FX 79-L-120) as shown in Fig. 9 it can be seen that FX-76-120 has a maximum power coefficient 0.2657 at TSR 2 and has a higher self-starting ability compared with other airfoils in FX-families.

![Figure 9. Cp vs. TSR for FX-Family](image)

**3.2.4 E-Family**

In this family, compared the performance of symmetric airfoils (E168, E169, E171, E474, and E475) as shown in Fig. 10 it can be seen that E169 has a maximum power coefficient of 0.3017 at TSR 2 and has a higher self-starting ability compared with other airfoils in E-families.
It clearly shows that the symmetrical airfoil section s1046 is the best compared with other airfoils (NACA 0018, E169, and FX 76-120).

4. Conclusion

- In this study, computer code using MATLAB program, based on the double-multiple stream tube (DMST) model, has been utilized for indicating the aerodynamic loads and performance of H-type Darrieus VAWT.
- Computer code based on the DMST model was successfully validated by comparing it to the data provided by the research literature.
- The power coefficient and self-starting behaviors of four families of symmetric airfoils (NACA00XX, S, FX, and E) were compared for low tip-speed ratios ranging from 0 to 4.5 at a low wind speed of 4 m/s.
- It clearly shows that the symmetrical airfoil section s1046 is the best compared with other airfoils that have shown the best performance in other families such as NACA 0018, E169, and FX 76-120.

Authors’ contribution

All authors contributed equally to the preparation of this article.

Declaration of competing interest

The authors declare no conflicts of interest.

Funding source

This study didn’t receive any specific funds.

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